

Spring School Trigonometry

1. Simplify the following expressions:

a)
$$\frac{\sin(315^\circ)\cos(-315^\circ)\sin(210^\circ)}{\tan(225^\circ)}$$

b)
$$\frac{8\cos^2 35^\circ - 8\sin^2 35^\circ}{2\sin 20^\circ}$$

2. Prove the following trig identities. You may ignore all restrictions

a)
$$\frac{\sin^3 x + \sin x \cos^2 x}{\cos x} = \tan x$$

b)
$$\cos^4 x - \sin^4 x = 2\cos^2 x - 1$$

c)
$$\frac{\sin 2x - \sin x}{\cos 2x + \cos x} = \frac{\sin x}{\cos x + 1}$$

3. Use the compound angle formulas to write each of the following as a single term

$$\sin 3\theta \cos \theta - \cos 3\theta \sin \theta$$

4. Evaluate the following without the use of a calculator

a) $\cos 105^\circ$

b) $\cos 230^\circ \cos 160^\circ + \sin 310^\circ \sin 200^\circ$

c) $\cos^2 15^\circ - \sin^2 15^\circ$

d) $1 - 2\sin^2 22,5^\circ$

5. Given that $\tan \theta = \frac{\sin 2\theta}{1 + \cos 2\theta}$

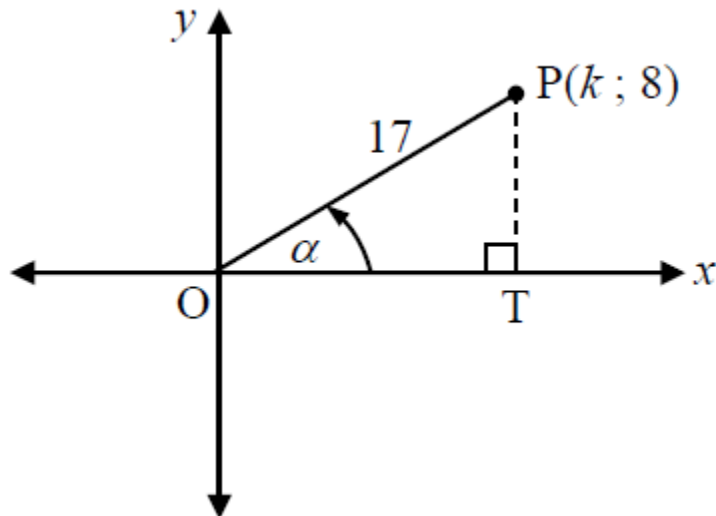
a) Prove the above identity.

b) Hence, determine the value of $\tan 22,5^\circ$ without the use of a calculator.

6. The point P(k;8) lies in the first quadrant such that OP = 17 units and $\angle TOP = \alpha$ as shown in the diagram below



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- a) Determine the value of k .
 - b) Write down the value of $\cos \alpha$.
 - c) If it is further given that $\alpha + \beta = 180^\circ$, determine, $\cos \beta$
 - d) Hence, determine the value of $\sin(\beta - \alpha)$
7. Answer the following question
- a) Prove $8\cos^4 x - 8\cos^2 x + 1 = \cos 4x$
 - b) Hence solve $8\cos^4 x - 8\cos^2 x + 1 = 0,8$
 - c) Express the following in terms of t , given $t = \sin \vartheta$

$$\frac{\cos(\vartheta - 90^\circ) \cos(720^\circ + \vartheta) \tan(\vartheta - 360^\circ)}{\sin^2(\vartheta + 360^\circ) \cos(\vartheta + 90^\circ)}$$

8. Answer the following question
- a) Prove that $\frac{1 - \cos 2x - \sin x}{\sin 2x - \cos x} = \tan x$
 - b) The above expression is undefined if $\sin 2x - \cos x = 0$. Solve this equation in the interval $0^\circ \leq x \leq 360^\circ$