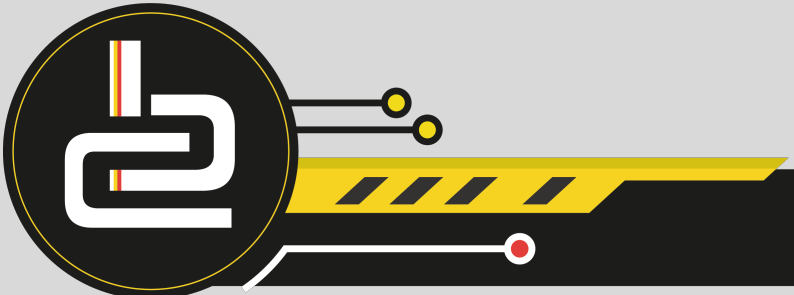




It's the way we're *wired*

GRADE 11 MATHS

Charmaine



FUNCTIONS

Functions of the form $y = mx + c$ are called straight line functions. In the equation, $y = mx + c$, m and c are constants and have different effects on the graph of the function.

m is the gradient

As m increases, the gradient of the graph increases.

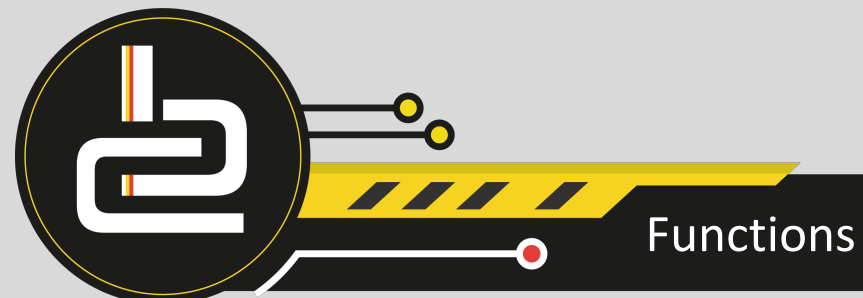
If $m > 0$ then the graph increases from left to right (slopes upwards).

If $m < 0$ then the graph increases from right to left (slopes downwards)

c is the y intercept

If $c > 0$ the graph shifts vertically upwards.

If $c < 0$ the graph shifts vertically downwards.

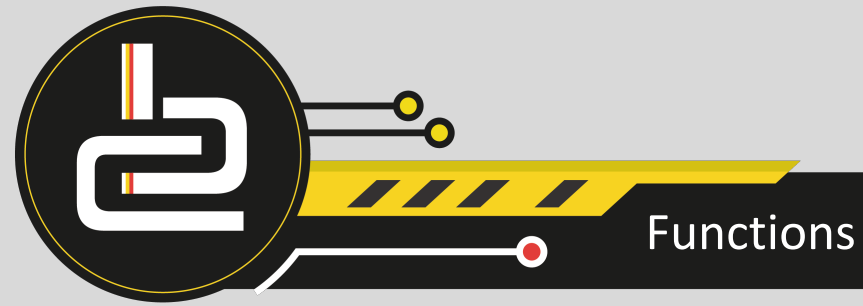


FUNCTIONS

Domain and range

The domain is $\{x : x \in \mathbb{R}\}$ because there is no value of x for which $f(x)$ is undefined.

The range of $f(x) = mx + c$ is also $\{f(x) : f(x) \in \mathbb{R}\}$ because $f(x)$ can take on any real value.



FUNCTIONS

Intercepts

The y -intercept:

Every point on the y -axis has an x -coordinate of 0. Therefore to calculate the y -intercept, let $x = 0$.

For example, the y -intercept of $g(x) = x - 1$ is given by setting $x = 0$:

$$\begin{aligned}g(x) &= x - 1 \\g(0) &= 0 - 1 \\&= -1\end{aligned}$$

This gives the point $(0; -1)$.

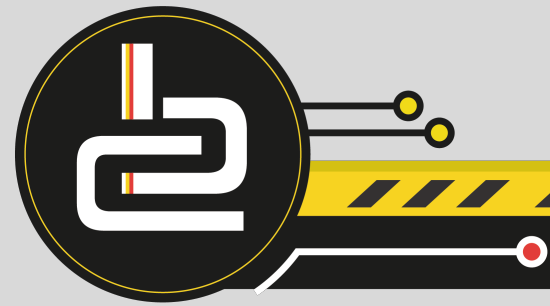
The x -intercept:

Every point on the x -axis has a y -coordinate of 0. Therefore to calculate the x -intercept, let $y = 0$.

For example, the x -intercept of $g(x) = x - 1$ is given by setting $y = 0$:

$$\begin{aligned}g(x) &= x - 1 \\0 &= x - 1 \\\therefore x &= 1\end{aligned}$$

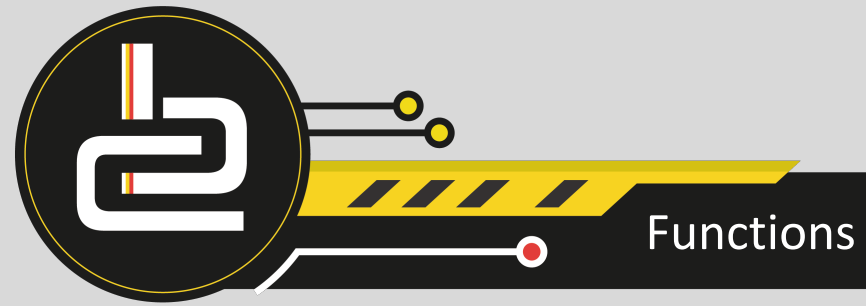
This gives the point $(1; 0)$.



FUNCTIONS

In order to sketch graphs of the form, $f(x) = mx + c$, we need to determine three characteristics:

1. sign of m
2. y -intercept
3. x -intercept



EXAMPLE: FUNCTIONS

Sketch the graph of $g(x) = x - 1$ using the dual intercept method

Step 1: Examine the standard form of the equation

In this example, $m = 1$ in other words $m > 0$. This means the graph increases as x increases

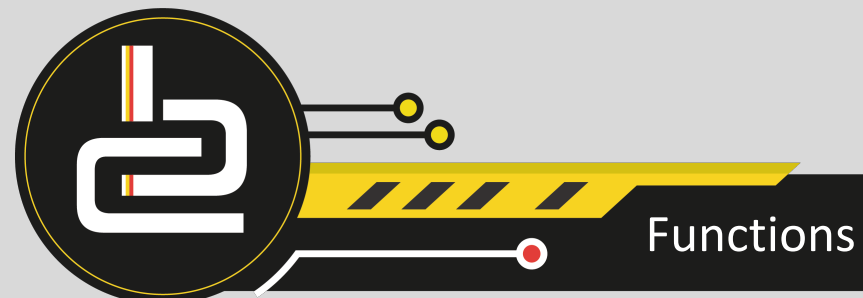
Step 2: Calculate the intercepts

For the y -intercept, let $x = 0$; therefore $g(0) = -1$.

This gives the point $(0; -1)$.

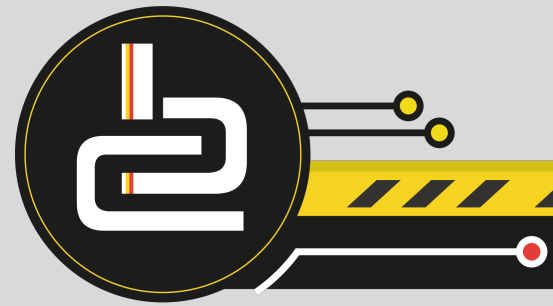
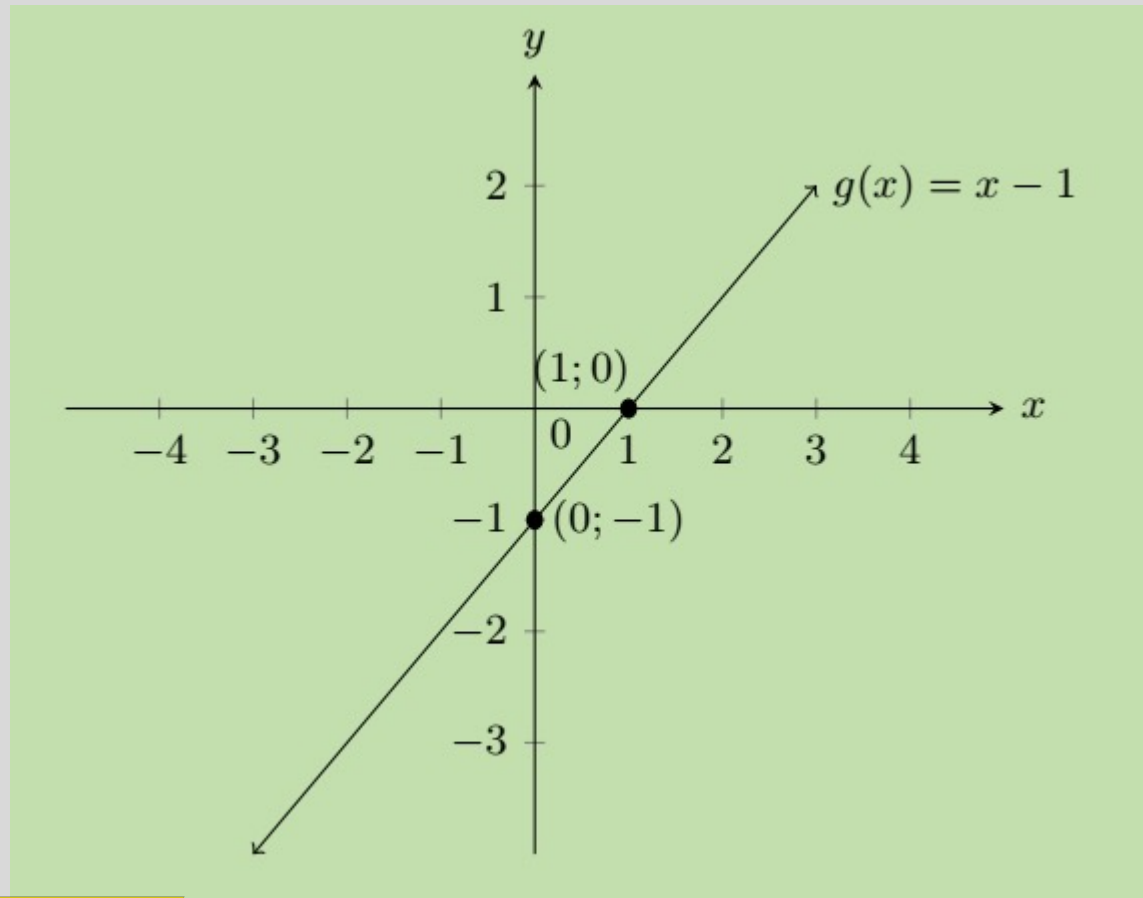
For the x -intercept, let $y = 0$; therefore $x = 1$.

This gives the point $(1; 0)$.



EXAMPLE: FUNCTIONS

Step 3: Plot the points and draw the graph



EXAMPLE: FUNCTIONS

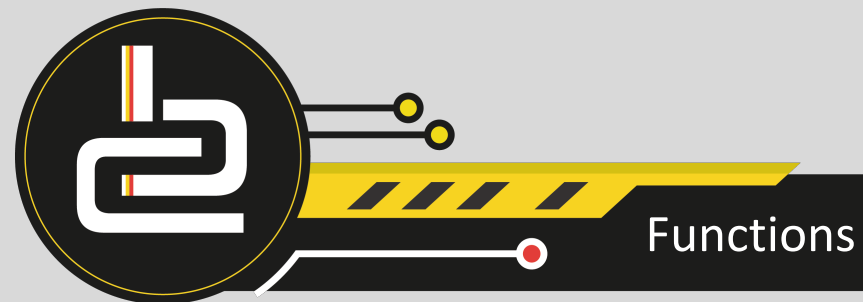
Sketch the graph of $p(x) = \frac{1}{2}x - 3$ using the gradient-intercept method.

Step 1: Use the intercept
 $c = -3$, which gives the point $(0; -3)$.

Step 2: Use the gradient

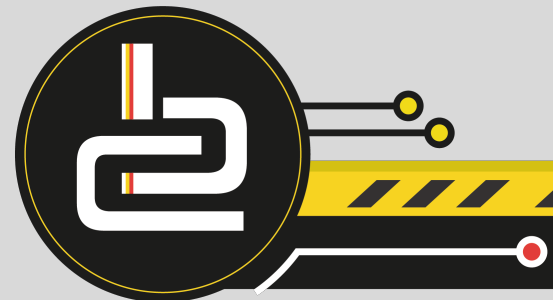
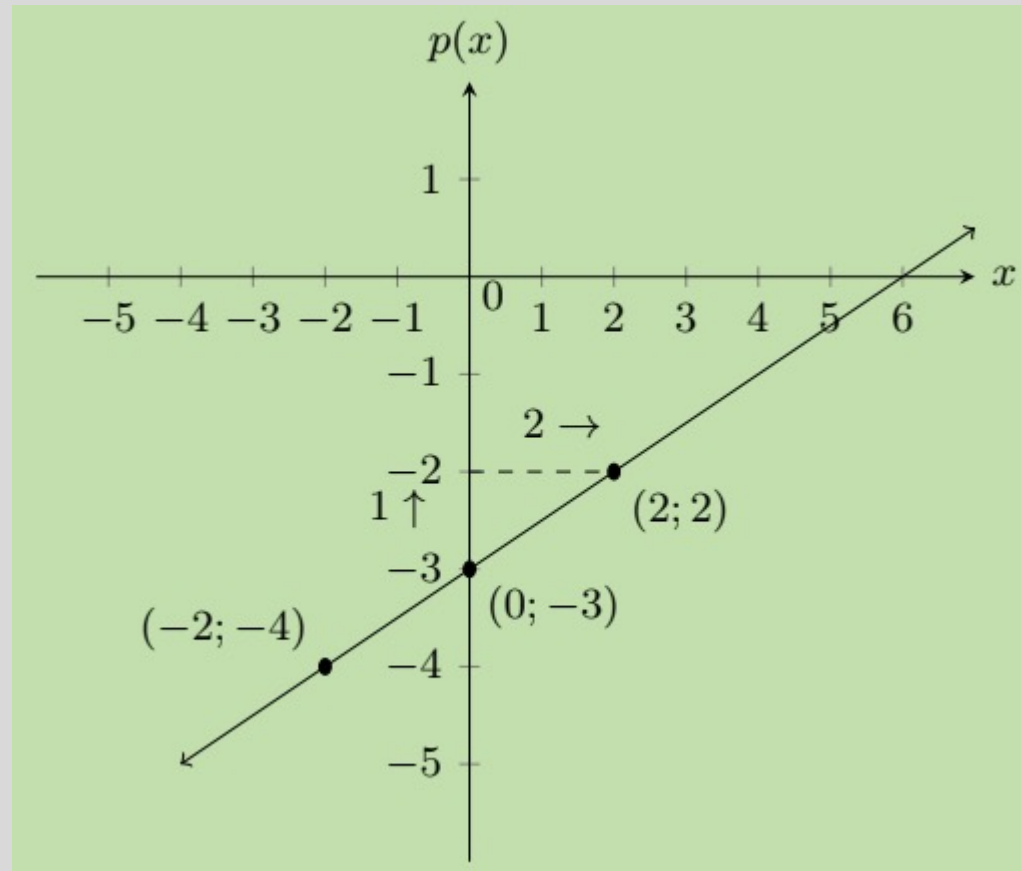
$$m = \frac{\text{change in } y}{\text{change in } x} = \frac{1}{2}$$

Start at $(0; -3)$. Move 1 unit up and 2 units to the right. This gives the second point $(2; -2)$.



EXAMPLE: FUNCTIONS

Step 3: Plot the points and draw the graph



EXERCISE: FUNCTIONS

1. Determine the x -intercept and the y -intercept of the following equations.

a) $y = x - 1$

b) $y = x + 2$

c) $y = x - 3$

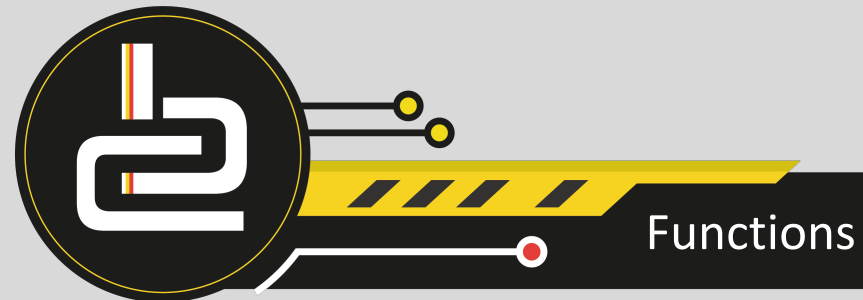
2. Write the following in standard form ($y = mx + c$):

a) $2y + 3x = 1$

b) $3x - y = 5$

c) $3y - 4 = x$

d) $y + 2x - 3 = 1$



EXERCISE: FUNCTIONS

3. Look at the graphs below. Each graph is labelled with a letter. In the questions that follow, match any given equation with the label of a corresponding graph.

a) $y = 5 - 2x$

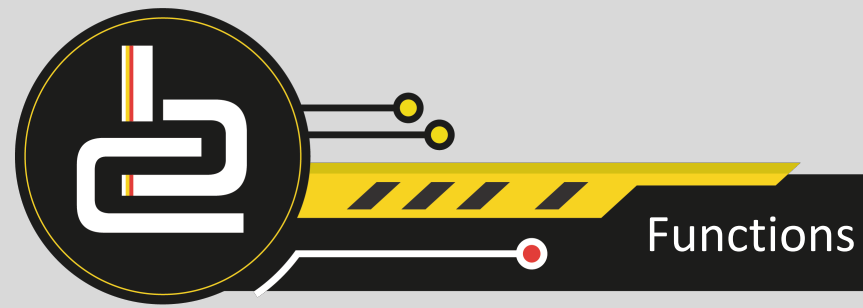
b) $x + 5$

c) $y = 2x - 6$

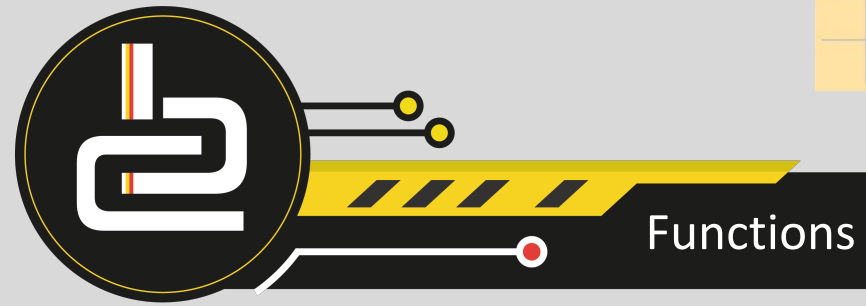
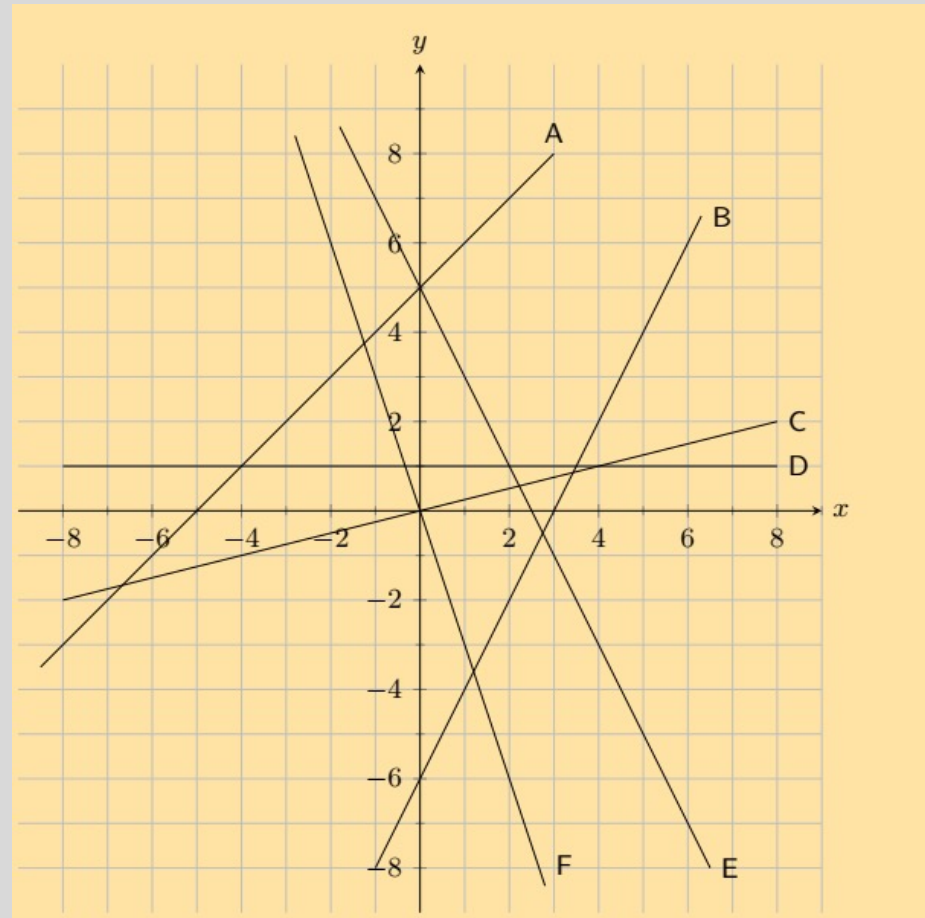
d) $y = -3x$

e) $y = 1$

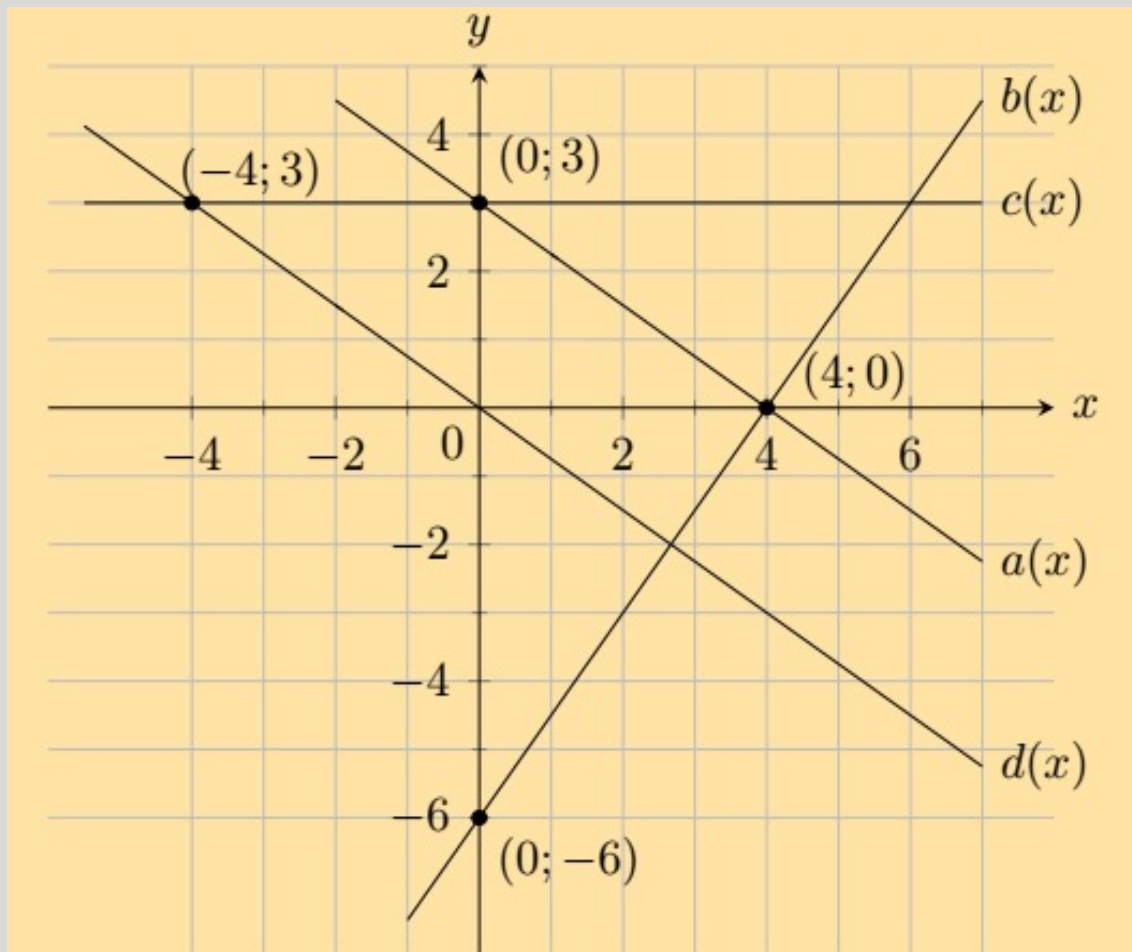
f) $y = \frac{1}{2}x$



FUNCTIONS



**FOR THE FUNCTIONS IN THE DIAGRAM BELOW,
GIVE THE EQUATION OF EACH LINE:**



SOLUTIONS: FUNCTIONS

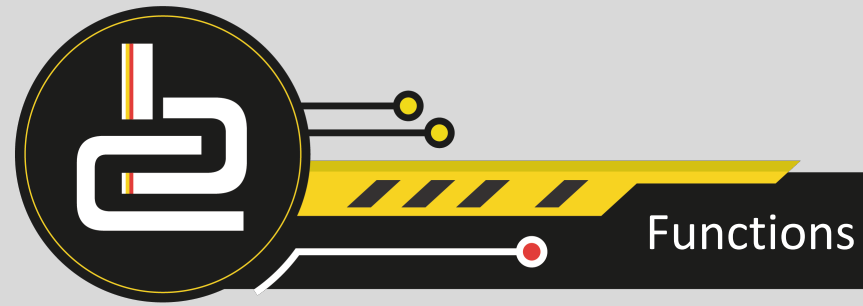
1. a) x -intercept = 1 and y -intercept = -1
b) x -intercept = -2 and y -intercept = 2
c) x -intercept = 3 and y -intercept = -3

2. a) $y = -\frac{3}{2}x + \frac{1}{2}$

- b) $y = -3x + 5$

- c) $y = \frac{1}{3}x + \frac{4}{3}$

- d) $y = -2x + 4$



SOLUTIONS: FUNCTIONS

3.

a) E
d) F

b) A
e) D

c) B
f) C

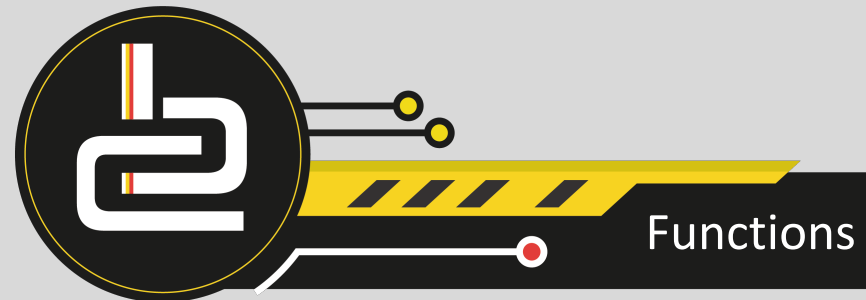
4.

$$a) a(x) = -\frac{3}{4}x + 3$$

$$b) b(x) = \frac{3}{2}x - 6$$

$$c) c(x) = 3$$

$$d) d(x) = -\frac{3}{4}x$$

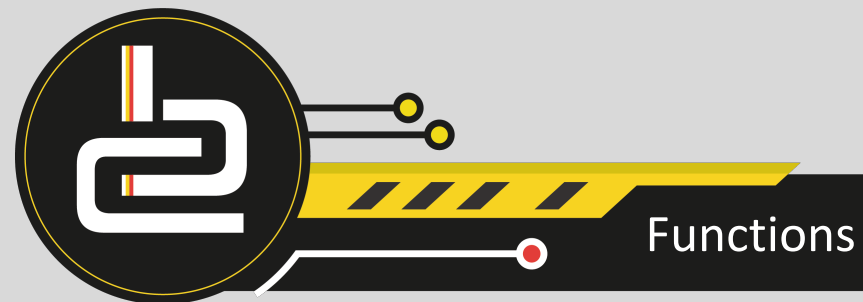


FUNCTIONS: INVERSE

The inverse of a function takes the y -values (range) of the function to the corresponding x -values (domain) and vice versa. Therefore the x and y values are interchanged.

The function is reflected along the line $y = x$ to form the inverse.

The notation for the inverse of a function is f^{-1} .



FUNCTIONS: INVERSE

Given $f(x) = 2x + 6$. Determine $f^{-1}(x)$. Sketch the graphs of $f(x)$, $f^{-1}(x)$ and $y = x$ on the same set of axis.

Step 1: Swap the x and y

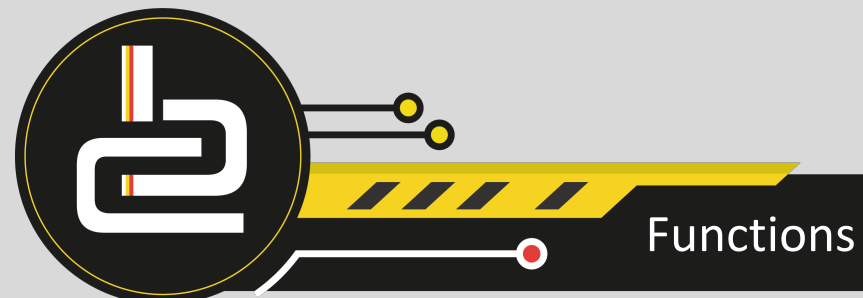
$y = 2x + 6$ becomes $x = 2y + 6$

Step 2: Make y the subject of the formula

$$2y = x - 6$$
$$y = \frac{1}{2}(x - 6)$$

$$y = \frac{1}{2}x - 3$$

$$\therefore f^{-1} = \frac{1}{2}x - 3$$



FUNCTIONS: INVERSE

Every point on the function has the same coordinates as the corresponding point on the inverse function, *except that they are swapped around*. For example: $(-3; 0)$ on the function is reflected to become $(0; -3)$ on the inverse function.

